Edexcel GCSE

Mathematics A

Paper 1 (Non-Calculator)

Higher Tier

Monday 11 June 2012 – Afternoon

Time: 1 hour 45 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser. Tracing paper may be used.

Instructions

• Use black ink or ball-point pen.
• Fill in the boxes at the top of this page with your name, centre number and candidate number.
• Answer all questions.
• Answer the questions in the spaces provided – there may be more space than you need.
• Calculators must not be used.

Information

• The total mark for this paper is 100
• The marks for each question are shown in brackets – use this as a guide as to how much time to spend on each question.
• Questions labelled with an asterisk (*) are ones where the quality of your written communication will be assessed.

Advice

• Read each question carefully before you start to answer it.
• Keep an eye on the time.
• Try to answer every question.
• Check your answers if you have time at the end.
Volume of prism = area of cross section × length

Area of trapezium = \( \frac{1}{2} (a + b)h \)

Volume of sphere = \( \frac{4}{3} \pi r^3 \)

Surface area of sphere = \( 4\pi r^2 \)

Volume of cone = \( \frac{1}{3} \pi r^2 h \)

Curved surface area of cone = \( \pi rl \)

In any triangle \( ABC \)

Sine Rule \( \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \)

Cosine Rule \( a^2 = b^2 + c^2 - 2bc \cos A \)

Area of triangle = \( \frac{1}{2} ab \sin C \)

The Quadratic Equation
The solutions of \( ax^2 + bx + c = 0 \) where \( a \neq 0 \), are given by
\[
x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}
\]
1 Sam wants to find out the types of film people like best.

He is going to ask whether they like comedy films or action films or science fiction films or musicals best.

(a) Design a suitable table for a data collection sheet he could use to collect this information.

Sam collects his data by asking 10 students in his class at school. This might not be a good way to find out the types of film people like best.

(b) Give one reason why.

(Total for Question 1 is 3 marks)
2. The diagram shows a patio in the shape of a rectangle.

![Diagram of a patio](image)

The patio is 3.6 m long and 3 m wide.

Matthew is going to cover the patio with paving slabs. Each paving slab is a square of side 60 cm.

Matthew buys 32 of the paving slabs.

(a) Does Matthew buy enough paving slabs to cover the patio?
   You must show all your working.

The paving slabs cost £8.63 each.

(b) Work out the total cost of the 32 paving slabs.

£ ..............................................

(Total for Question 2 is 6 marks)
Bill uses his van to deliver parcels.
For each parcel Bill delivers there is a fixed charge plus £1.00 for each mile.
You can use the graph to find the total cost of having a parcel delivered by Bill.

(a) How much is the fixed charge?

£ ..............................................  (1)

Ed uses a van to deliver parcels.
For each parcel Ed delivers it costs £1.50 for each mile.
There is no fixed charge.

(b) Compare the cost of having a parcel delivered by Bill with the cost of having a parcel delivered by Ed.

(Total for Question 3 is 4 marks)
Here are the speeds, in miles per hour, of 16 cars.

<table>
<thead>
<tr>
<th>Speed</th>
</tr>
</thead>
<tbody>
<tr>
<td>31</td>
</tr>
<tr>
<td>52</td>
</tr>
<tr>
<td>43</td>
</tr>
<tr>
<td>49</td>
</tr>
<tr>
<td>36</td>
</tr>
<tr>
<td>35</td>
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<tr>
<td>33</td>
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<tr>
<td>29</td>
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<tr>
<td>54</td>
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<tr>
<td>43</td>
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<tr>
<td>44</td>
</tr>
<tr>
<td>46</td>
</tr>
<tr>
<td>42</td>
</tr>
<tr>
<td>39</td>
</tr>
<tr>
<td>55</td>
</tr>
<tr>
<td>48</td>
</tr>
</tbody>
</table>

Draw an ordered stem and leaf diagram for these speeds.

(Total for Question 4 is 3 marks)
You can work out the amount of medicine, $c \text{ ml}$, to give to a child by using the formula

$$c = \frac{ma}{150}$$

$m$ is the age of the child, in months.
$a$ is an adult dose, in ml.

A child is 30 months old.
An adult’s dose is 40 ml.

Work out the amount of medicine you can give to the child.

$\text{.............................................. ml}$

(Total for Question 5 is 2 marks)
Here are the ingredients needed to make 12 shortcakes.

Liz makes some shortcakes.
She uses 25 ml of milk.

(a) How many shortcakes does Liz make?

Robert has 500 g of sugar
1000 g of butter
1000 g of flour
500 ml of milk

(b) Work out the greatest number of shortcakes Robert can make.

(Total for Question 6 is 4 marks)
7 Buses to Acton leave a bus station every 24 minutes.  
Buses to Barton leave the same bus station every 20 minutes.  
A bus to Acton and a bus to Barton both leave the bus station at 9:00 am.  
When will a bus to Acton and a bus to Barton next leave the bus station at the same time?

8 (a) Expand $3(2y - 5)$

(b) Factorise completely $8x^2 + 4xy$

(c) Make $h$ the subject of the formula

\[ t = \frac{gh}{10} \]

\[ h = \frac{10t}{g} \]
Describe fully the single transformation that maps triangle A onto triangle B.

(Total for Question 9 is 3 marks)
**10** Railtickets and Cheaptrains are two websites selling train tickets.

Each of the websites adds a credit card charge and a booking fee to the ticket price.

<table>
<thead>
<tr>
<th>Railtickets</th>
<th>Cheaptrains</th>
</tr>
</thead>
<tbody>
<tr>
<td>Credit card charge: 2.25% of ticket price</td>
<td>Credit card charge: 1.5% of ticket price</td>
</tr>
<tr>
<td>Booking fee: 80 pence</td>
<td>Booking fee: £1.90</td>
</tr>
</tbody>
</table>

Nadia wants to buy a train ticket.
The ticket price is £60 on each website.
Nadia will pay by credit card.

Will it be cheaper for Nadia to buy the train ticket from Railtickets or from Cheaptrains?

(Total for Question 10 is 4 marks)
The diagram shows a parallelogram. The sizes of the angles, in degrees, are

\[2x\]
\[3x - 15\]
\[2x\]
\[2x + 24\]

Work out the value of \(x\).
12 Jane has a carton of orange juice. 
The carton is in the shape of a cuboid.

The depth of the orange juice in the carton is 8 cm.

Jane closes the carton. 
Then she turns the carton over so that it stands on the shaded face.

Work out the depth, in cm, of the orange juice now.

.............................................. cm

(Total for Question 12 is 3 marks)
The diagram shows a regular hexagon and a regular octagon.

Calculate the size of the angle marked $x$.
You must show all your working.

(Total for Question 13 is 4 marks)
The diagram shows the position of a lighthouse \( L \) and a harbour \( H \).

The scale of the diagram is 1 cm represents 5 km.

(a) Work out the real distance between \( L \) and \( H \).

.............................................. km

(1)

(b) Measure the bearing of \( H \) from \( L \).

..............................................°

(1)

A boat \( B \) is 20 km from \( H \) on a bearing of 040°.

(c) On the diagram, mark the position of boat \( B \) with a cross (\( \times \)). Label it \( B \).

(2)

(Total for Question 14 is 4 marks)
Harry grows tomatoes.
This year he put his tomato plants into two groups, group A and group B.

Harry gave fertiliser to the tomato plants in group A.
He did not give fertiliser to the tomato plants in group B.

Harry weighed 60 tomatoes from group A.
The cumulative frequency graph shows some information about these weights.

(a) Use the graph to find an estimate for the median weight.

.............................................. g

(1)
The 60 tomatoes from group A had a minimum weight of 153 grams and a maximum weight of 186 grams.

(b) Use this information and the cumulative frequency graph to draw a box plot for the 60 tomatoes from group A.

Harry did not give fertiliser to the tomato plants in group B.

Harry weighed 60 tomatoes from group B. He drew this box plot for his results.

(c) Compare the distribution of the weights of the tomatoes from group A with the distribution of the weights of the tomatoes from group B.

(Total for Question 15 is 6 marks)
16 (a) Simplify $(m^2)^5$

..............................................  
(1)

(b) Factorise $x^2 + 3x - 10$

..........................................................................  
(2)

(Total for Question 16 is 3 marks)

17 (a) Write down the value of $10^9$

..............................................  
(1)

(b) Write $6.7 \times 10^{-5}$ as an ordinary number.

..............................................  
(1)

(c) Work out the value of $(3 \times 10^7) \times (9 \times 10^9)$
Give your answer in standard form.

..............................................  
(2)

(Total for Question 17 is 4 marks)
Triangle $ABC$ is drawn on a centimetre grid.
$A$ is the point $(2, 2)$.
$B$ is the point $(6, 2)$.
$C$ is the point $(5, 5)$.

Triangle $PQR$ is an enlargement of triangle $ABC$ with scale factor $\frac{1}{2}$ and centre $(0, 0)$.

Work out the area of triangle $PQR$.

\[
\text{cm}^2
\]

(Total for Question 18 is 3 marks)
19 Wendy goes to a fun fair.
She has one go at Hoopla.
She has one go on the Coconut shy.

The probability that she wins at Hoopla is 0.4
The probability that she wins on the Coconut shy is 0.3

(a) Complete the probability tree diagram.

(b) Work out the probability that Wendy wins at Hoopla and also wins on the Coconut shy.

(Total for Question 19 is 4 marks)
20. Solve the simultaneous equations

\[
\begin{align*}
5x + 2y &= 11 \\
4x - 3y &= 18
\end{align*}
\]

\[
x = \ldots \\
y = \ldots
\]

(Total for Question 20 is 4 marks)
B, C and D are points on the circumference of a circle, centre O. 
AB and AD are tangents to the circle.

Angle $DAB = 50^\circ$

Work out the size of angle $BCD$.
Give a reason for each stage in your working.

(Total for Question 21 is 4 marks)
The table gives some information about the speeds, in km/h, of 100 cars.

<table>
<thead>
<tr>
<th>Speed (s km/h)</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>$60 &lt; s \leq 65$</td>
<td>15</td>
</tr>
<tr>
<td>$65 &lt; s \leq 70$</td>
<td>25</td>
</tr>
<tr>
<td>$70 &lt; s \leq 80$</td>
<td>36</td>
</tr>
<tr>
<td>$80 &lt; s \leq 100$</td>
<td>24</td>
</tr>
</tbody>
</table>

(a) On the grid, draw a histogram for the information in the table.

![Histogram](image)

(b) Work out an estimate for the number of cars with a speed of more than 85 km/h.

\[
\text{Estimated number of cars} = 15 + 25 = 40
\]

(Total for Question 22 is 5 marks)
23 (a) Simplify fully \( \frac{x^2 + 3x - 4}{2x^2 - 5x + 3} \)

(b) Write \( \frac{4}{x + 2} + \frac{3}{x - 2} \) as a single fraction in its simplest form.

(Total for Question 23 is 6 marks)

24 Express the recurring decimal 0.2\( \overline{8} \) as a fraction in its simplest form.

(Total for Question 24 is 3 marks)
25 The diagram shows a solid metal cylinder.

The cylinder has base radius $2x$ and height $9x$.

The cylinder is melted down and made into a sphere of radius $r$.

Find an expression for $r$ in terms of $x$. 

Diagram NOT accurately drawn
The graph of $y = f(x)$ is shown on each of the grids.

(a) On this grid, sketch the graph of $y = f(x - 3)$
(b) On this grid, sketch the graph of \( y = 2f(x) \)

(Total for Question 26 is 4 marks)